### Firing Missiles at Right Angles to Reality: The Search for Hidden Dimensions of Nature

#### An ex-Higgs-Hunter's Guide to Extra Dimensions and the Quest for Physics Beyond the Standard Model



Physics Colloquium Syracuse University Jay Hubisz Sept 19, 2013



"..anyone who has been to the higher dimensions will know that they're a pretty nasty heathen lot up there who should just be smashed and done in, and would be, too, if anyone could work out a way of firing missiles at right-angles to reality." -Douglas Adams Hitchhiker's guide to the galaxy

### Take me to your leader



# Take me to your leader

## Take me to your leader



RULER

Feynman: We can use hydrogen atoms as our common ruler



Use fundamental constants to work in terms of single unit Mass/Energy

Speed of light - convert meters to seconds, kg to GeV  $c=3\cdot 10^8 {\rm m/s} ~~E=mc^2$ 

Planck's constant - convert seconds to GeV  $\hbar = 6.6 \cdot 10^{-25} GeV \cdot s$ Everything can be measured in terms of GeV ~ I M<sub>Proton</sub>

### We have lots of Rulers



You can't just make things bigger and expect them to work the same way Nature is full of different length scales The scales we observe follow from violations of scale invariance at the shortest distances



### Some physics in Feynman's answer

Height:  
Height:  
Bohr Radius: 
$$a_0 = \frac{4\pi}{e^2 m_e}$$
  
Electron Charge Electron mass (Higgs)  
MProton~I GeV  
Mass:  
Mass:  
Meroton Chromodynamics  
theory of quarks and gluons  
Theorem different dynamical phonomenon contribute to

Iwo very different dynamical phenomena contribute to volume-mass relations of every-day objects

#### our local universe



some other hospitable corner of the multiverse

#### What's a hydrogen atom?

### One Ruler to Rule them all

We both live in spacetime - should both have gravity

$$V = -\frac{G_N M_1 M_2}{r}$$
  
GeV = [V] = [G\_N]GeV<sup>3</sup>  $\rightarrow$  [G\_N] =  $\frac{1}{\text{GeV}^2}$   
 $G_N = \frac{1}{M_{\text{Planck}}^2}$ 

$$M_{\rm Planck} = \sqrt{\frac{\hbar c}{G_N}} \approx 10^{19} {\rm GeV} \qquad L_{\rm Planck}$$

 $L_{\rm Planck} \approx 10^{-35} {\rm m}$ 

We're 3x10<sup>105</sup> Planck lengths in volume Our mass is 4x10<sup>29</sup> Planck masses



What will their response be?



# What are the ways in which you can move?

### Effective Field Theory

#### Ken Wilson (1936-2013)



The greatest physicist the average person has never heard of

### Effective Field Theory systems w/ fluctuations at all scales

Quantum Field Theory sum over all possible fluctuations long and short wavelength included

$$Z = \int D\phi \exp\left[\frac{i}{\hbar}S\right]$$

Function S (the action) contains all the physics Z is generating function for QM amplitudes Useful in condensed matter - approach to phase transitions

### Effective Field Theory Parameters

Relationship between parameters in action and physical observables is complicated

e.g. a very simple quantum field theory:

$$S = \int d^4x \left[ \frac{1}{2} (\partial_\mu \phi)^2 - m^2 \phi^2 - \lambda \phi^4 \right]$$
$$m_{\rm obs}^2 = m_{\rm obs}^2 (m^2, \lambda)$$

Parameters in action wildly different from observables Summing over all scales:  $m^2$  and  $\lambda$  must both be infinite to get finite  $m^2_{Obs}$ Cumbersome juggling of infinities to get out real physics



#### "Dragons" at high momentum:

infinities, string theory/quantum gravity, GUT's, stuff that might solve SM problems...

#### Don't sweat the small stuff

Perform integral over high momentum fields first!  $Z = \int [D\phi_{<}] [D\phi_{>}] \exp\left[\frac{i}{\hbar}S\right] = \int [D\phi_{<}] \exp\left[\frac{i}{\hbar}\tilde{S}\right]$   $\tilde{S}$  is "effective" action valid for all scales below  $\Lambda_{\rm UV}$ 

You don't need to know what's going on up there! Your mission is to construct an **effective** action with **finite** parameters describing what you **do** see

$$\alpha(\Lambda_{UV}), M_{\text{Higgs}}(\Lambda_{UV}), \text{etc...}$$

ergy/Momentum scales

### The Wilsonian Ruler

### $I/\Lambda_{UV}$ is a **length scale** we can measure all of our dimensionful parameters in units of it

 $M_{\rm Higgs}^2 = c_{\rm Higgs} \Lambda_{\rm UV}^2 \qquad \qquad \Lambda_{\rm CC} = c_{\Lambda} \Lambda_{\rm UV}^4$ 

This ruler is fictitious when you already know S a convention

BUT

when curtain nears a threshold where there is new physics UV cutoff takes on physical meaning

Example: Scale at which gravitational coupling grows big!

#### As we push the boundaries of the **energy frontier**, we push the UV cutoff ever higher finite parameters of effective action change

Wilsonian view of renormalization group:  $\alpha(\Lambda_{UV}) \to \alpha(\Lambda'_{UV}) \qquad M_{\text{Higgs}}(\Lambda_{UV}) \to M_{\text{Higgs}}(\Lambda'_{UV})$   $\frac{c_i^{(n)}(\Lambda_{UV})}{\Lambda_{UV}^n} \to \frac{c_i^{(n)}(\Lambda'_{UV})}{\Lambda'_{UV}^n}$ 

#### Rule:

all predictions for the low energy processes you've already probed must remain identical

"Dragons" hide in parameters  $c_i^{(n)}(\Lambda_{\rm UV})$ with negative mass dimension:  $\Lambda_{UV}^n$  $\frac{c_i^{(n)}(\Lambda_{\rm UV})}{\Lambda_{\rm UV}^n} \to \frac{c_i^{(n)}(\Lambda_{\rm UV}')}{\Lambda_{\rm UV}'^n}$ If you measure a  $c \neq 0$ , it grows **quickly** signals onset of non-perturbativity/New Physics Fermi Theory  $\implies$  Electroweak theory Dragons = W<sup>±</sup>, Z bosons Bad behavior of W scattering  $\implies$  Higgs discovery Dragon = Higgs boson As we push the boundaries of the intensity frontier, we push the c's ever smaller (or discover non-zero ones!)

$$S = \int d^4x \left[ \frac{1}{2} (\partial_\mu \phi)^2 - m^2 \phi^2 - \lambda \phi^4 \right]$$

action must be dimensionless to be in exponential

$$Z = \int D\phi \exp\left[\frac{i}{\hbar}S\right]$$

$$[\partial_{\mu}] = \text{GeV} \qquad [dx] = \text{GeV}^{-1}$$

so: 
$$[\phi] = \text{GeV} \quad [\phi^4] = \text{GeV}^4$$
  
and:  $[\lambda] = 1$  Right?

$$S = \int d^4x \left[ \frac{1}{2} (\partial_\mu \phi)^2 - m^2 \phi^2 - \lambda \phi^4 \right]$$

action must be dimensionless to be in exponential

$$Z = \int D\phi \exp\left[\frac{i}{\hbar}S\right]$$

 $[\partial_{\mu}] = \text{GeV} \qquad [dx] = \text{GeV}^{-1}$ 

So: 
$$[\phi] = \text{GeV} \quad [\phi^4] = \text{GeV}^4$$

#### and: $[\lambda] = 1$ WRONG (but close if $\lambda$ is small)

"Unlike for everyone else, I+I isn't I, for us it is more like 4." -Yuval Grossman

Naive dimensional analysis doesn't capture all the physics

$$\frac{d\lambda}{d\log\Lambda_{\rm UV}} = \beta(\lambda) \longleftarrow {\rm smal}$$
$$\lambda(\Lambda_{\rm UV}) = \lambda_0 \Lambda_{\rm UV}^{\beta(\lambda_0)/\lambda_0}$$

"Dimensionless" coupling constants change with scale

If  $\beta$  is positive,  $\lambda$  grows (like the c's) If  $\beta$  is negative,  $\lambda$  shrinks

### "Emergent" scales

For theory of quarks and gluons  $\beta$  is negative

Running the procedure in reverse - lowering the curtain:



### Standard Model vs Wilsonian Standard Model

As a fundamental theory:



Pathologies all in "bare" parameters cumbersome order by order (in perturbation theory) subtraction of infinities

# Standard Model vs Wilsonian Standard Model

As a Wilsonian Effective Field Theory

$$\begin{aligned} \mathcal{L}_{\Lambda} &= -\frac{1}{4g_s^2(\Lambda)} G^2 - \frac{1}{4g_w^2(\Lambda)} W^2 - \frac{1}{4g_y^2(\Lambda)} B^2 + \mu^2(\Lambda) |H|^2 - \lambda(\Lambda) |H|^4 + \text{fermions} \\ &+ \sum_i \frac{c_i(\Lambda) \mathcal{O}_i(\Lambda)}{\Lambda^n} \end{aligned}$$

All parameters are finite - study approach to pathologies in controlled and phenomenologically motivated way and they have real physical meaning!

### The Standard Model Fermions

<b>FERMIONS</b> matter constituents spin = 1/2, 3/2, 5/2,							
Leptons spin =1/2				Quarks spin =1/2			
Flavor	Mass GeV/c <sup>2</sup>	Electric charge		Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge	
V lightest neutrino*	(0-0.13)×10 <sup>-9</sup>	0		U up	0.002	2/3	
electron	0.000511	-1		d down	0.005	-1/3	
VMmiddle neutrino*	(0.009-0.13)×10 <sup>-9</sup>	0		C charm	1.3	2/3	
μ muon	0.106	-1		S strange	0.1	-1/3	
VHheaviest neutrino*	(0.04-0.14)×10 <sup>-9</sup>	0		t top	173	2/3	
τ tau	1.777	-1		b bottom	4.2	-1/3	

# Standard Model Bosons

**BOSONS** force carriers spin = 0, 1, 2, ...

Unified Electroweak spin = 1						
Name	Mass GeV/c <sup>2</sup>	Electric charge				
<b>Y</b> photon	0	0				
W	80.39	—1				
	80.39	+1				
W bosons	91.188	0				
Z boson						

Strong (color) spin =1						
Name	Mass GeV/c <sup>2</sup>	Electric charge				
g	0	0				
gluon						

+ HIGGS BOSON M<sub>H</sub>~126 GeV Charge = 0

### The Standard Model

b

Cd

v's

g





# No nearby obvious pathologies

"The Standard Model is a really good effective theory" -Simon Catterall

### Almost every hep-ex paper:

"The data are consistent with Standard Model expectations, and limits are set..."



"I think you ought to know I'm feeling very depressed" -Marvin the paranoid android



"Incredible... It's even worse than I thought it would be."









In particle physics:  $\frac{j}{j_c} - 1 \sim 10^{-32} \sim \left(\frac{M_{\text{weak}}}{M_{\text{planck}}}\right)^2$ Masses would generically be of order MPlanck or MGUT Nature 487, 454–458 (26 July 2012)

## Fine Tuning in Wilsonian Picture

sum over all fluctuations  $M_{\rm Obs}^2 = c_{\rm Higgs} \Lambda_{\rm UV}^2 + relevant$  for this measurement up to scale  $\Lambda_{UV}$ top higgs microscopics above the curtain  $-\frac{3}{8\pi^2}\lambda_t^2\Lambda^2$ top loop  $\frac{9}{64\pi^2}g^2\Lambda^2$ SU(2) gauge boson loops  $\frac{1}{16\pi^2}\lambda^2\Lambda^2$ Higgs loop

 $c_{Higgs}$  tuned to part in  $M_{Higgs}^2/\Lambda_{UV}^2$ 

## Strong CP Problem

#### QCD "should" have violated CP

neutron electric dipole moment - sensitive to both strong and weak CP violating phases  $\mathcal{L}_{\rm CP} = \theta G \cdot G$  $\bar{\theta} = \theta - \arg \det M_a$  — This part is from the Higgs! must be  $< 10^{-11}!$ One of the best solutions so far New particle: Axion Vaxion minimized when strong CP violation vanishes > only QCD can contribute...another tuning!

(Planck scale is actually TOO SMALL here)

### Cosmological Constant ∧<sub>cc</sub>≃(10<sup>-12</sup> GeV)<sup>4</sup>

Just as the Higgs fills the vacuum with weak-charge, it also fills it with an energy density

$$V(\langle H \rangle) = V_0 - \frac{\mu^4}{4\lambda} \approx (10^2 \,\text{GeV})^4$$
  
56 orders of magnitude!!??

There are also a bunch of quantum contributions that seem to greatly exacerbate the problem also other contributions of similar style (i.e. QCD)
## Fermion masses



#### These come from the Higgs

 $\sum \lambda_{ij} H \psi_L^i \psi_R^j$ 

Neutrinos are special  $\sum \frac{1}{\Lambda} \lambda_{ij} \nu_i^T H i \tau 2 H \nu_j$ 

- very small #'s or very high scale

## Flavor

Weak interactions are not diagonal

#### e.g. top-bottom, top-strange, top-down



 $J = (2.91^{+0.19}_{-0.11}) \times 10^{-5}$  - weak CP violation

This is close to the identity, and very hierarchical off-diagonals quantify amount of flavor changing in weak interactions

weak charge and masses **almost** simultaneously diagonalizable...why?

## What does the Higgs not do?

- It doesn't give masses of order M<sub>Planck</sub>
  - It should
- It doesn't give huge contribution to Evacuum
  - It should
- It doesn't give huge contribution to strong CP violation
  - It should
- It doesn't give generically large flavor changing couplings
   It should



A New Mechanism for Hierachical Scale Generation, Naturally Light Scalar Fields, and Naturally Suppressed CC

Bellazzini, Csaki, JH, Serra, Terning arXiv:1305.3919 "A Naturally Light Dilaton and a small Cosmological Constant" Eur.Phys.J. C73 (2013) 2333 "A Higgs-like Dilaton" and ongoing research

## Moving about

#### Recall how we formally move about in physics



commutation relations specify the actions Can construct theories symmetric under these actions

# In space-timeTurnTranslateBoost $J_i$ in space: $P_i$ $K_i$ in time: HK

$$[J_i, J_j] = i \epsilon_{ijk} J_k ,$$
  

$$[J_i, K_j] = i \epsilon_{ijk} K_k ,$$
  

$$[K_i, K_j] = -i \epsilon_{ijk} J_k ,$$
  

$$[J_i, P_j] = i \epsilon_{ijk} P_k ,$$
  

$$[K_i, P_j] = -iH \delta_{ij} ,$$
  

$$[J_i, H] = [P_i, H] = [H, H] = (0)$$
  

$$[K_i, H] = -i P_i ,$$

More possibilities in QFT? Coleman-Mandula Theorem says NO

### Scale invariance (aka conformal invariance)

A way to avoid Coleman-Mandula: Give up on having an analytic scattering matrix

$$\begin{split} &[J_i, J_j] = i \epsilon_{ijk} J_k , \qquad + \\ &[J_i, K_j] = i \epsilon_{ijk} K_k , \\ &[K_i, K_j] = -i \epsilon_{ijk} J_k , \\ &[J_i, P_j] = i \epsilon_{ijk} P_k , \\ &[K_i, P_j] = -i H \delta_{ij} , \\ &[J_i, H] = [P_i, H] = [H, H] = 0 , \\ &[K_i, H] = -i P_i , \end{split}$$

+ Generator for changing rulers  $[D, P_{\mu}] = P_{\mu}$ 

 $e^{i\lambda D}x_{\mu} = e^{\lambda}x_{\mu}$ 

At energies above  $m_{Higgs}$  the SM is nearly scale invariant

## "Biggest" Problem:

When QCD phase transition occurs (or any other PT's occur in early universe - e.g. Higgs) vacuum filled with energy density (cosmological constant)

History of the CC:



Supersymmetry really can't do much about this one



Pathology manifests when denominator vanishes



approach to phase transition Scale invariance very broken near I GeV! Determined by value of QCD coupling constant at the highest scales (e.g. MGUT or MPlanck)

#### UV boundary conditions determine IR scale

Could there be a theory where the IR scale is sensitive to the eventual value of the CC itself? An adjustment mechanism?

## Spontaneously broken symmetries



Symmetry appears as "mysterious" relations among parameters in effective action & conspicuously light particles

#### Example:

#### Below QCD phase transition

Light pions and  $g_{\pi NN}f_{\pi} = G_{N^0}M_N$  (to about 10%)

#### pion-nucleon coupling

decay rate of neutron

We have since developed procedures to construct effective theories where symmetry is manifest

## pontaneously broken Scale Invariance?

$$S_{\text{eff}} = \int d^4x \frac{1}{2} (\partial \chi)^2 - a\chi^4$$
$$\langle \chi \rangle = f$$

#### **Obstruction:**

• 
$$a > 0 \rightarrow f = 0$$
 (no breaking)

Fubini '76

- $a < 0 \rightarrow f = \infty$  (runaway)
  - $a = 0 \rightarrow f = anything (flat potential)$ (massless particle - no symmetry)

a is cosmological constant in units of f! CC problem - it's usually big

 $f = \infty$ 



Hard to realize

## Spontaneously broken almost scale invariance

quartic coupling "a" depends on parameters of UV theory

 $a(\lambda)$  is function with zero for some value of  $\lambda$ 

If theory is not quite scale invariant, coupling  $\lambda$  can change slowly

$$\frac{d\lambda}{d\log\mu} = \epsilon$$

so quartic (Cosmological constant) changes with scale!  $a(\lambda(\chi))\chi^4$ 

No longer a simple quartic potential



## Where do extra dimensions come in?

$$[J_i, J_j] = i \epsilon_{ijk} J_k , \qquad +$$
  

$$[J_i, K_j] = i \epsilon_{ijk} K_k , ,$$
  

$$[K_i, K_j] = -i \epsilon_{ijk} J_k , ,$$
  

$$[J_i, P_j] = i \epsilon_{ijk} P_k , ,$$
  

$$[K_i, P_j] = -iH \delta_{ij} , ,$$
  

$$[J_i, H] = [P_i, H] = [H, H] = 0$$
  

$$[K_i, H] = -i P_i , ,$$

- Generator for changing rulers  $[D, P_{\mu}] = P_{\mu}$ 

 $e^{i\lambda D}x_{\mu} = e^{\lambda}x_{\mu}$ 

These are the **same** as the movements in a 5D space with constant negative curvature quantum field theories in these 5D spaces share properties with certain scale invariant 4D theories (AdS/CFT) Changes in scale = translations in 5th dimension

## 5D Model that implements ideas of cartoon

arXiv:1305.3919 "A Naturally Light Dilaton and a small Cosmological Constant"

5D Gravity + single scalar field w/ small potential (small  $\epsilon$ )

$$\ddot{\phi} + \left[4\dot{\phi} + \frac{6}{\kappa^2}\frac{\partial\log V}{\partial\phi}\right]\left[1 - \frac{\kappa^2}{12}\dot{\phi}^2\right] = 0$$

$$\sim \log \lambda$$

IR contributions from phase transitions go here

Ζ

TeV scale

Planck scale

system responds by shifting Planck scale - CC stays zero

## Can we observe this? Some speculation/outlook:

• Gravity waves/CMB: phase transitions in early universe

- dynamics of true vacuum bubble collisions sensitive to this mechanism!
- Neutron stars: Seems like there should be order I change in energy density in exotic phases in core
  - mass-radius relations and/or limits may be affected!
- Dark-Matter: Light scalar may undergo coherent oscillations after phase transitions
  - correspondence between Dark Matter and Dark Energy?
    - Strong tie-in to cosmic frontier

## Problem One

#### Still need enormous tuning here

#### We fixed the tuning here

#### How is potential kept small?

Ζ

TeV scale

Planck scale

### Another Coleman-Mandula Loophole:

$$\begin{split} & [J_i, J_j] = i \epsilon_{ijk} J_k , \\ & [J_i, K_j] = i \epsilon_{ijk} K_k , \\ & [K_i, K_j] = -i \epsilon_{ijk} J_k , \\ & [J_i, P_j] = i \epsilon_{ijk} P_k , \\ & [K_i, P_j] = -i H \delta_{ij} , \\ & [J_i, H] = [P_i, H] = [H, H] = 0 , \\ & [K_i, H] = -i P_i , \end{split}$$

All commutation relations

anti-commutation relations?

$$\{Q_{\alpha}, Q_{\dot{\alpha}}^{\dagger}\} = 2\sigma^{\mu}_{\alpha\dot{\alpha}}P_{\mu}$$

truly quantum dimensions: can only take one step in each one

Supersymmetry is an extra-dimensional theory



#### 5D Gravity + single scalar field w/ small potential (small €) + supersymmetry

 $\phi \sim \log \lambda$ 

Planck scale z TeV scale (Supersymmetric) (no SUSY) system responds by shifting Planck scale - CC stays zero

## Problem Two

#### The Planck scale is **TOO SMALL**



Recall our best solution to the strong CP problem has same issue!

## What don't these 5D Models do?

- They don't give masses of order M<sub>Planck</sub>
  - Randall, Sundrum '99
- The don't give huge contribution to Evacuum
  - (Bellazzini, Csáki, JH, Serra, Terning 2013)
- They don't give huge contribution to strong CP violation
  - Adding SUSY may give axion for strong CP
  - also see (Bunk, JH 2010)
- They don't give fermion masses all at weak scale
  - Grossman, Neubert '99

They don't give generically large flavor changing couplings

• many interesting works on flavor (Cornell, Harvard, Maryland)

## Phenomenological Consequences

Energy Frontier: New resonances associated with extra dimensional dynamics, changes in Higgs physics (e.g. ongoing work with Jain, Bunk + many new features given most recent work)

Intensity Frontier: Flavor physics predictions are affected (will be different in our new construction - future work)

Cosmic Frontier: Gravity waves, observations of neutron stars, dark matter puzzle, general cosmological evolution (ongoing research Bellazzini, Csáki, JH, Redi, Serra, Terning)

## We seem to slowly be getting better at painting our own self portrait





#### We're 3x10<sup>105</sup> Planck lengths in volume Our mass is 4x10<sup>29</sup> Planck masses and we move in 3 space dimensions, 1 time....



"Whoa...you are a very spacious species"

OR....

...plus one curved dimension and a couple intrinsically quantum dimensions plus .....

"Sounds about par for the course."

## Thank You!